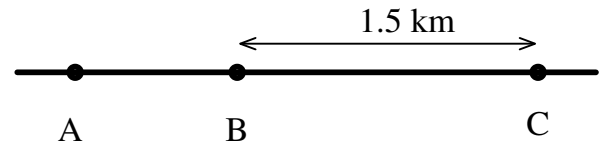


## MIDTERM 1 2009 SUMMER

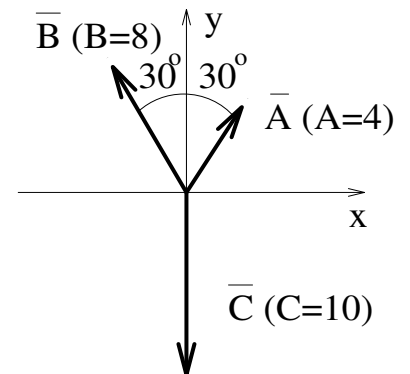
*Solve the following problems*

1. A car starts from rest to move from point A to point B with constant acceleration. It arrives to B after 25 s with a velocity of 30 m/s. It moves further from B toward point C with unchanged velocity (30 m/s). Calculate the average velocity of the car (in m/s) during its way from A to C.



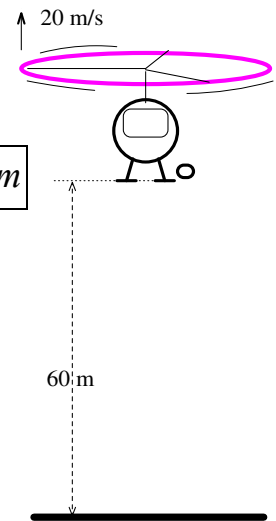
$$\bar{v} = \frac{\Delta x_1 + \Delta x_2}{\Delta t_1 + \Delta t_2} = \frac{\bar{v} \Delta t_1 + \Delta x_2}{\Delta t_1 + \Delta x_2 / v_2} = \frac{15 \text{ m/s} \cdot 25 \text{ s} + 1500 \text{ m}}{25 \text{ s} + 1500 \text{ m} / 30 \text{ m/s}} = 25 \text{ m/s}$$

2. Three vectors  $\vec{A}$ ,  $\vec{B}$ , and  $\vec{C}$  are shown in the figure. Find the magnitude and direction of the sum vector  $\vec{D} = \vec{A} + \vec{B} + \vec{C}$ .



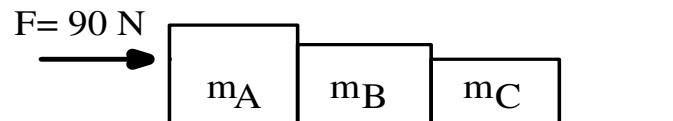
$$\begin{aligned} A_x &= 4 \cos 60 = 2; & A_y &= 4 \sin 60 = 3.46 \\ B_x &= 8 \cos 120 = -4; & B_y &= 8 \sin 120 = 6.928 \\ C_x &= 10 \cos 270 = 0 & C_y &= 10 \sin 270 = -10 \\ D_x &= 2 - 4 + 0 = -2 \\ D_y &= 3.46 + 6.928 - 10 = 0.388 \\ D &= \sqrt{D_x^2 + D_y^2} = 2.037 \\ \theta &= \tan^{-1} \frac{D_y}{D_x} = -11^\circ \\ \theta &= 180^\circ + \tan^{-1} \frac{D_y}{D_x} = 180^\circ + (-11^\circ) = 169^\circ \end{aligned}$$

3. A helicopter is ascending at a constant velocity 20 m/s, as shown. At a height of 60 m a package is dropped from the helicopter. **Find the distance between the helicopter and the package 4s after the package is released.**



$$\Delta y = \Delta y_{helic} - \Delta y_{stone} = +(v_0 t) - (v_0 t + at^2 / 2) = 20m/s \cdot 4s - 0 = 80m$$

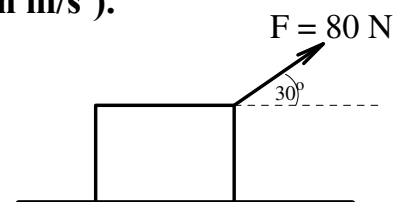
4. Three masses  $m_A = 8$  kg,  $m_B = 6$  kg, and  $m_C = 4$  kg are in contact on a frictionless table. A horizontal force is applied on  $m_A$ , as shown in the figure. **Find the net force (in N) acting on  $m_B$ .**



The masses can be treated as one mass of 18 kg, so

$$F = ma \rightarrow a = \frac{F}{m} = \frac{90N}{18kg} = 5m/s \Rightarrow F_B = m_B a = 6kg \cdot 5m/s = 30N$$

5. A 12-kg box is pulled with a 80-N force as shown in the figure. The kinetic friction coefficient is  $\mu_k = 0.3$ . **Calculate the acceleration of the box (in  $m/s^2$ ).**



$$F_y^{net} : F_N + F_p \sin 30 - mg = 0 \Rightarrow F_N = mg - F_p \sin 30 = 120N - 40N = 80N$$

$$F_x^{net} : F_p \cos 30 - F_{fr} = F_p \cos 30 - \mu F_N = 69.28N - 0.3 \cdot 80N = 45.28N = ma$$

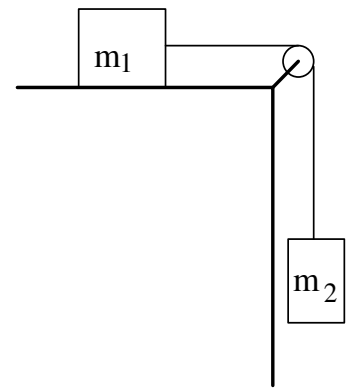
$$\Rightarrow a = \frac{45.28N}{12kg} = 3.77m/s^2$$

6. Two masses  $m_1 = 4 \text{ kg}$  and  $m_2 = 6 \text{ kg}$  are connected via a massless cord and pulley.  $m_1$  moves on a frictionless table. **Find the acceleration of  $m_1$  (in  $\text{m/s}^2$ ).**

$$m_1: T = m_1 a \quad (1)$$

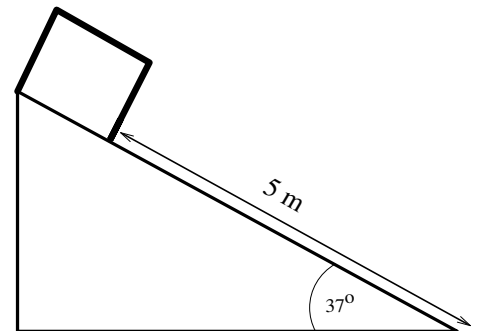
$$m_2: -T + m_2 g = m_2 a \quad (2)$$

$$(1)+(2): m_2 g = (m_1 + m_2) a \Rightarrow a = \frac{m_2 g}{m_1 + m_2} = 6 \text{ m/s}^2$$



7. A box of mass  $m = 15 \text{ kg}$  starting from rest slides down along the  $5 \text{ m}$  long incline. **Calculate the velocity at which the box reaches the bottom of the incline (in  $\text{m/s}$ ).** The kinetic friction coefficient between the box and the incline is  $\mu_k = 0.3$ .

$$a = g \sin 37^\circ - \mu g \cos 37^\circ = 3.6 \text{ m/s}^2 \Rightarrow v^2 = v_0^2 + 2a\Delta x \Rightarrow v = \sqrt{2a\Delta x} = 6 \text{ m/s}$$



8. A mass of  $3 \text{ kg}$  is in uniform circular motion around a horizontal circle of radius  $R = 3 \text{ m}$ . It makes 20 full rotations in 1 minute. **Find the magnitude of net force (in  $\text{N}$ ) that keeps the body in circular motion.**

$$T = 60 \text{ s} / 20 = 3 \text{ s}$$

$$F = ma = m \frac{v^2}{R} = m \frac{(2\pi R)^2}{T^2 R} = 39.5 \text{ N}$$