



**Kuwait University**

**Physics Department**

**Physics 102**

**Second Midterm Examination**

**Spring Semester (2010 - 2011)**

**May 14, 2011**

**Time: 12:00 –13:30 PM**

**Name.....Student No.....**

**Instructors:** Drs. Abdel-Karim, Afrousheh, Davis, Farhan, Habib, Kokaj, Lajko, Rakhshani, Rao, Razee, and Sharma

**(Fundamental constants)**

- $k = \frac{1}{4\pi\epsilon_0} = 9.0 \times 10^9 \text{ N}\cdot\text{m}^2 / \text{C}^2$  (Coulomb constant)
- $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2 / (\text{N}\cdot\text{m}^2)$  (Permittivity of free space)
- $\mu_0 = 4\pi \times 10^{-7} \text{ T}\cdot\text{m/A}$  (Permeability of free space)
- $|e| = 1.60 \times 10^{-19} \text{ C}$  (Elementary unit of charge)
- $N_A = 6.02 \times 10^{23}$  (Avogadro's number)
- $g = 9.8 \text{ m/s}^2$  (Acceleration due to gravity)
- $m_e = 9.11 \times 10^{-31} \text{ kg}$  (Electron mass)
- $m_p = 1.67 \times 10^{-27} \text{ kg}$  (Proton mass)

**Prefixes of units**

- $m = 10^{-3}$        $\mu = 10^{-6}$        $n = 10^{-9}$        $p = 10^{-12}$
- $k = 10^3$        $M = 10^6$        $G = 10^9$        $T = 10^{12}$

**For use by Instructors only**

Prob.	1	2	3	4	5	6	7	8	Total
Marks									

Ques.	1	2	3	4	5	6	7	8	Total
Marks									

**Important Notes:**

1. Do not start your exam until you are told to do so.
2. Answer all problems, show your work and mark your final answer.
3. Your work in this booklet should be neatly presented.
4. Books, notes and mobile phones are not allowed during the exam.
5. You may use a non-programmable calculator.

**Good Luck**

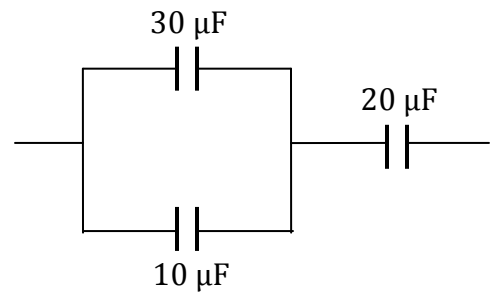
1. In the system of capacitors shown below, the total energy stored is  $60 \mu\text{J}$ . Determine the charge on the  $30 \mu\text{F}$  capacitor. [4 Points]

$$C_{eq} = \frac{40}{3} \mu\text{F}$$

$$U = \frac{Q^2}{2C_{eq}} \rightarrow Q = 40 \mu\text{C}$$

$$V = \frac{Q}{(30 \mu\text{F} + 10 \mu\text{F})} = 1 \text{ V}$$

$$Q_{30} = 30 \times 1 = 30 \mu\text{C}$$



2. A capacitor  $C_1$  is charged to a potential of  $100 \text{ V}$ . After it is disconnected from the source,  $C_1$  is then connected to an uncharged capacitor  $C_2 = 60 \mu\text{F}$ . If the final potential difference across the  $60 \mu\text{F}$  capacitor is  $40 \text{ V}$ , determine  $C_1$ . [3 points]

$$Q_{total} = C_1 \times 100$$

$$Q_{total} = (C_1 + C_2) \times 40$$

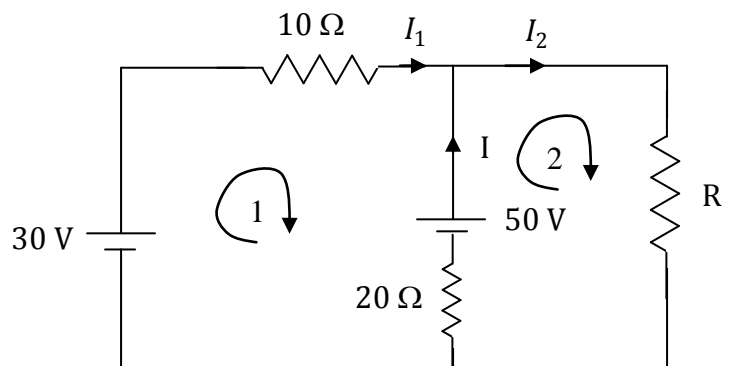
$$2.5C_1 = C_1 + C_2 \rightarrow C_1 = 40 \mu\text{F}$$

3. In the circuit shown below, the current  $I$  is  $1.5 \text{ A}$ . Determine the resistance  $R$ . [4 Points]

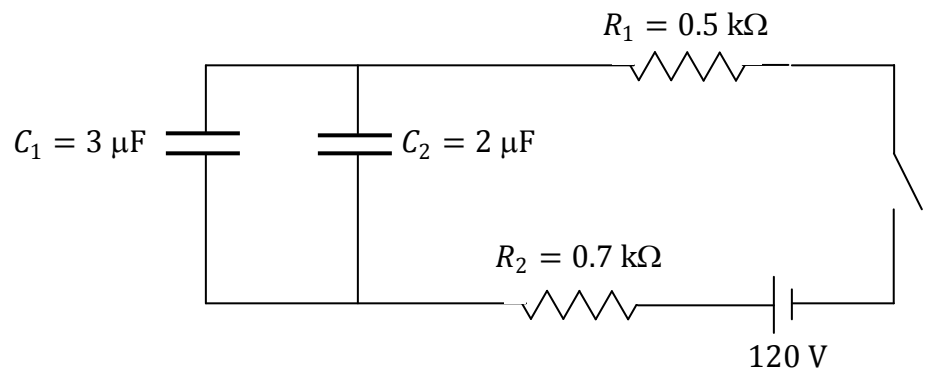
Junction:  $I_2 = I_1 + I$

Loop (1)  $I_1 = 1 \text{ A}$   
 $I_2 = 2.5 \text{ A}$

Loop (2)  $R = 8.0 \Omega$



4. The capacitors in the circuit shown below are initially uncharged. The switch is closed at  $t = 0$ . Determine the plate charge of capacitor  $C_1$  at time  $t = 2 \text{ ms}$ . [4 Points]



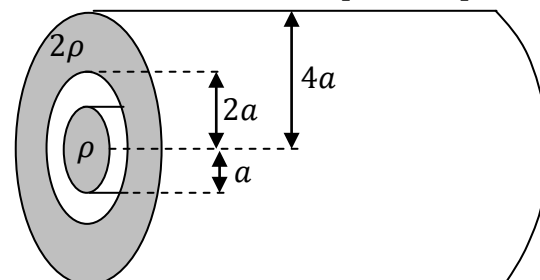
$$R = 1.2 \text{ k}\Omega, \quad C = 5 \mu\text{F}$$

$$Q = \varepsilon C (1 - e^{-t/RC}) = 170 \mu\text{C}$$

$$V_1 = V_2 = \frac{Q}{C} = 34 \text{ V}$$

$$Q_1 = V_1 \times C_1 = 102 \mu\text{C}$$

5. A conducting cylindrical wire of radius  $r_1 = a$ , resistivity  $\rho$  and length  $L$  is surrounded by a coaxial cylindrical shell of inner radius  $r_2 = 2a$ , outer radius  $r_3 = 4a$ , resistivity  $2\rho$  and length  $L$  as shown in the figure. [4 Points]



- a) Write down the resistance of the wire with radius  $r_1$ .

$$R_1 = \frac{\rho L}{\pi a^2}$$

- b) Write down the resistance of the cylindrical shell.

$$R_2 = \frac{2\rho L}{\pi(16a^2 - 4a^2)} = \frac{\rho L}{6\pi a^2}$$

- c) Show that the resistance of the system of two conductors is given by  $R = \frac{\rho L}{7\pi a^2}$ .

$$\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2}$$

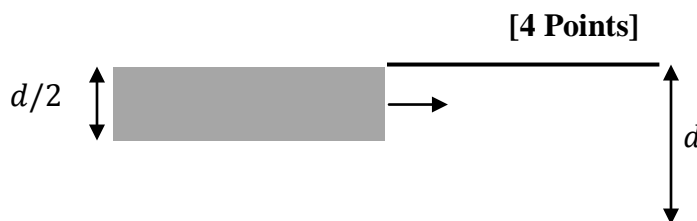
$$R = \frac{\rho L}{7\pi a^2}$$

6. A parallel-plate capacitor  $C_0$  of plate area  $A$  and separation  $d$  is connected to a battery and has the stored energy of  $6 \mu\text{J}$ . While the battery is still connected, a dielectric slab of area  $A$ , thickness  $d/2$  and dielectric constant  $K = 3$  is inserted between the plates. Determine the final stored energy. [4 Points]

V is constant

$$C = \frac{3}{2}C_0$$

$$U_{\text{after}} = \frac{1}{2}CV^2 = \frac{3}{2}U_{\text{before}} = 9 \mu\text{J}$$

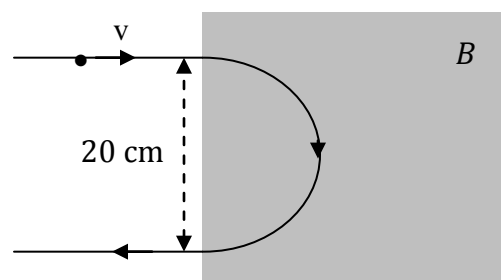


7. A proton is accelerated from rest through a potential difference of  $10 \text{ kV}$ . It then enters a region having a uniform magnetic field  $\vec{B}$  and exits the region as shown in the figure. Find the magnitude and direction of the magnetic field  $\vec{B}$ . [5 Points]

$$\frac{1}{2}mv^2 = qV \rightarrow v = 1.38 \times 10^6 \text{ m/s}$$

$$R = \frac{mv}{qB} \rightarrow B = 0.14 \text{ T}$$

$B$  is outward



8. An electron with velocity  $\vec{v} = 5.0 \times 10^5 \hat{j} \text{ m/s}$  is at a point where the electric field is  $\vec{E} = (3.0 \times 10^4 \hat{i} - 4.0 \times 10^4 \hat{j}) \text{ N/C}$  and the magnetic field is  $\vec{B} = 2.0 \times 10^{-2} \hat{i} \text{ T}$ . At that instant, what is the magnitude of the net force on the electron? [4 Points]

$$\vec{F}_{\text{electric}} = q\vec{E} = -e(3.0 \times 10^4 \hat{i} - 4.0 \times 10^4 \hat{j}) \text{ N}$$

$$\vec{F}_{\text{magnetic}} = q\vec{v} \times \vec{B} = e 10^4 \hat{k} \text{ N}$$

$$F = e(\sqrt{1 + 9 + 16}) \times 10^4 = 8.2 \times 10^{-15} \text{ N}$$

## Conceptual Questions

1. When a dielectric ( $K$ ) is inserted inside a capacitor, the stored energy increases by a factor of 2. What is the ratio of the electric fields before and after the dielectric is inserted?

- a)  $K$
- b)  $1/K$
- c) 2
- d) 1

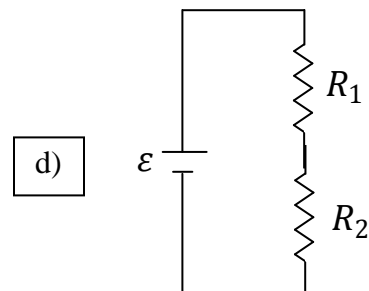
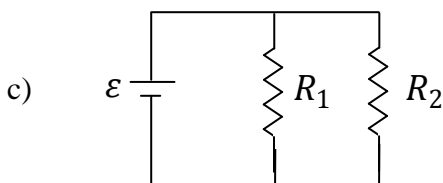
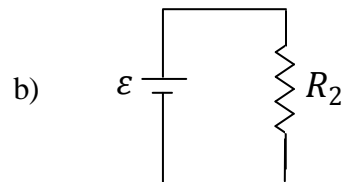
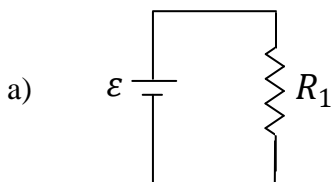
2. The identical circular plates of a capacitor ( $C_1$ ) are a distance  $d$  apart. The radius of each plate is  $r$ . If  $r$  is **increased** by a factor of 2 and  $d$  is **decreased** by a factor of 2, the new capacitance is

- a)  $C_1$
- b)  $\frac{1}{2}C_1$
- c)  $8C_1$
- d)  $2C_1$

3. The electrical conduction properties of copper and rubber are different because

- a) positive charges can move in copper but not in rubber.
- b) electrons can move in copper but not in rubber.
- c) positive charges can move in rubber but not in copper.
- d) electrons can move in rubber but not in copper.

4. If  $R_1 > R_2$ , in which of the following four circuits is the power dissipation lowest?

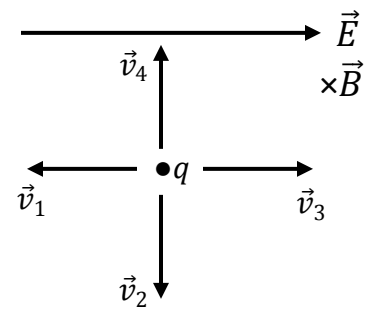


5. Kirchoff's loop rule:

- a) cannot be used in loops with capacitors.
- b) can only be used in loops with batteries.
- c) can be used in any loop provided it is closed.
- d) cannot be used if the current changes with time.

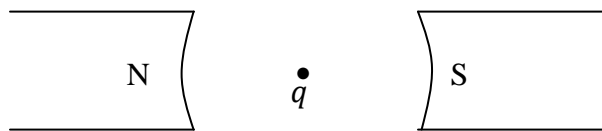
6. A point charge  $q$  can be launched with four different velocities inside a region of perpendicular electric and magnetic fields. For which velocity can the total force on charge  $q$  be zero?

- a)  $\vec{v}_1$
- b)  $\vec{v}_2$
- c)  $\vec{v}_3$
- d)  $\vec{v}_4$



7. An electron is placed at rest between two poles of a permanent magnet as shown below. The magnetic force acting on the electron is

- a) zero.
- b) towards N.
- c) towards S.
- d) upward.



8. In the circuit shown below the capacitor is initially uncharged. The current,  $I_0$ , through resistor  $R_1$  just after switch  $S$  is closed is

- a)  $I_0 = \frac{\epsilon}{R_1 + R_2}$ .
- b)  $I_0 = \frac{\epsilon}{R_1}$ .
- c)  $I_0 = \frac{\epsilon}{R_2}$ .
- d) zero.

