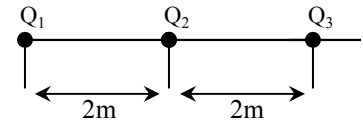




**Part - I**

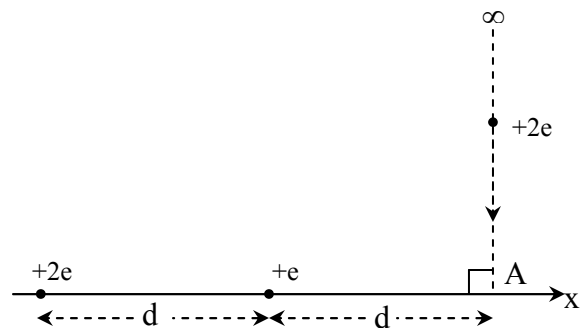
1. Three equal, point charges  $Q_1, Q_2, Q_3$  are placed along a straight line, with the distance between neighbouring charges being 2 m as shown in figure below. If  $Q_1 = Q_2 = Q_3$  & the magnitude of the net force acting on charge  $Q_3$  is 1.125N. What is the magnitude of the charge? (2 points)



$$k \frac{q^2}{(4^2)} + k \frac{q^2}{(2^2)} = 1.25N$$

$$q = 20\mu C$$

2. In the figure a particle of charge  $+2e$  is moved in from infinity to a point  $A$  on the x-axis. How much work is done if the distance  $d = 4m$ . (2 points)



Calculating the net potential at A

Calculating the work

$$W = \frac{1}{4\pi\epsilon_0} \left[ \frac{(2e)(2e)}{2d} + \frac{2e(e)}{d} \right] = \frac{e^2}{\pi\epsilon_0 d}$$

$$W = 2.3 \times 10^{-28} J$$

3. In the figure  $C_1 = C_2 = C_4 = 8\mu\text{F}$  and  $C_3 = 4\mu\text{F}$ . What is the potential difference across  $C_4$ ?

(2 points)

$$\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2} \Rightarrow C_{12} = 4\mu\text{f}$$

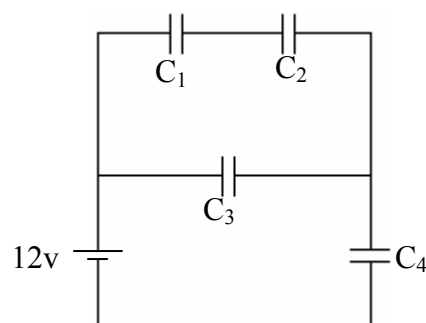
$$C_{123} = C_{12} + C_3$$

$$C_4 = C_{123}$$

$$q_T = C_{1234} \cdot 12V$$

$$V_4 = \frac{q_T}{8\mu\text{F}}$$

$$\mathbf{V = 6V}$$



4. In the circuit shown,  $\mathcal{E}$  is the emf and  $r$  is its internal resistance. The circuit has a current of 0.5A when  $R = 10\Omega$  and a current of 0.27A when  $R = 20\Omega$ . Find the emf  $\mathcal{E}$  of battery.

(3 points)

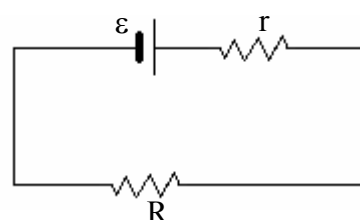
$$I_1 = \frac{\mathcal{E}}{R_1 + r}$$

$$I_2 = \frac{\mathcal{E}}{R_2 + r}$$

$$\frac{I_1}{I_2}; r = 1.74\Omega$$

$$\mathcal{E} = I(R + r)$$

$$\mathbf{\mathcal{E} = 5.9V}$$



5. Find the currents  $I_1$ ,  $I_2$ ,  $I_3$  and  $I_4$  in the circuit shown.

(4 Points)

$$6 - 6 - 10I_4 = 0,$$

$$I_4 = 0$$

$$+6 - 3I_1 - 3 = 0$$

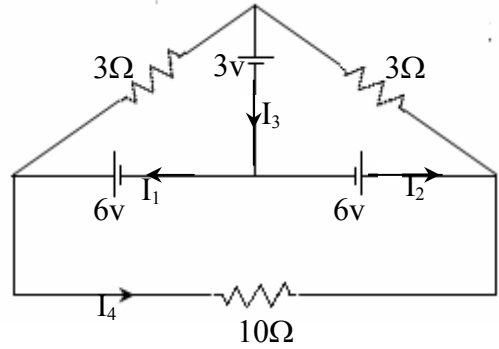
$$I_1 = 1\text{A}$$

$$-6 + 3 + 3I_2 = 0$$

$$I_2 = +1\text{A}$$

$$I_1 + I_2 = I_3$$

$$I_3 = 2\text{A}$$



6. A parallel plate capacitor has plate area  $A$  & plate separation  $d=4\text{cm}$ . A dielectric slab of area  $A$  & width  $w = d/4$  is placed against the positively charged plate. The positive plate is at 100 V & the negative plate at 0 V. Calculate the voltage at the air-dielectric interface S if the dielectric constant is  $K = 3$ .

(3 points)



$$100 = V_A + V_K$$

$$C_A V_A = C_K V_K$$

$$V_K = 10\text{V}$$

$$V_A = 100\text{V} - 10\text{V}$$

$$= 90\text{V}$$

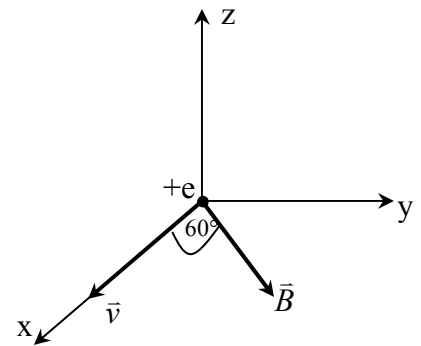
7. A proton moves with a speed of  $8 \times 10^6 \text{ m/s}$  along the x axis. It enters a region where there is a magnetic field of magnitude 2.5T, directed at angle of  $60^\circ$  to x-axis and lying in xy plane as shown in the figure. What are the magnitude and direction of the initial acceleration of the proton?

(3 points)

$$\vec{F} = q \vec{v} \times \vec{B}$$

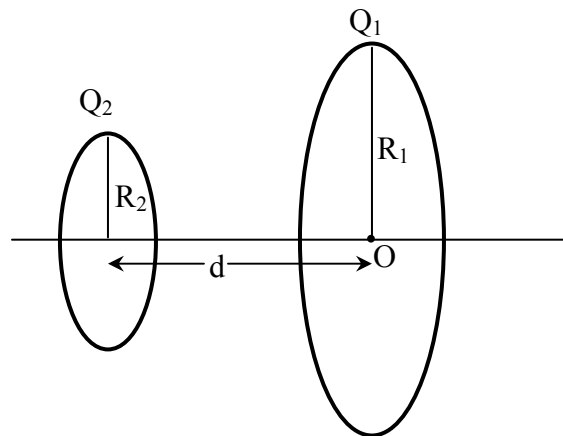
$$\vec{a} = \frac{qvB \sin \theta}{m} \vec{k}$$

$$a = 1.7 \times 10^{15} \text{ m/s}^2$$



8. Two rings of radii  $R_1 = 0.2 \text{ m}$  &  $R_2 = 0.1 \text{ m}$  carrying charges  $Q_1 = 200 \mu\text{C}$ ,  $Q_2 = -400 \mu\text{C}$  have a common axis & are aligned parallel to each other with their centers being separated by a distance of  $d = 1 \text{ m}$  (see figure). Determine the magnitude & direction of the electric field at the center O of the larger ring.

(3 points)



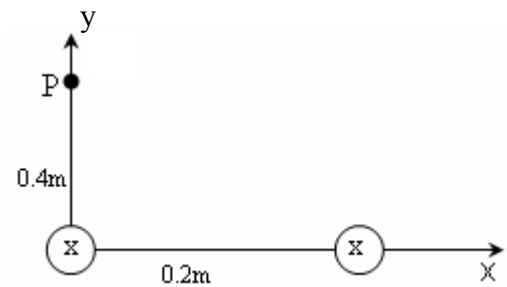
$$E_1 = 0$$

$$E_2 = \frac{Q_2 d}{4\pi\epsilon_0 (d^2 + R_2^2)^{3/2}} = 3.5 \times 10^6 \frac{\text{N}}{\text{C}}$$

Direction: along the axis to the left.

9. Two long straight wires perpendicular to the xy-plane, as shown in the fig., carry equal currents of 5A. Find components of  $\vec{B}$  at the point P(0,0.4m) on the y-axis.

(4 points)



$$B_1 = \frac{\mu_0 I}{2\pi(0.4)} = 2.5 \mu T$$

$$B_2 = \frac{\mu_0 I}{2\pi\sqrt{0.2}} = 2.24 \mu T$$

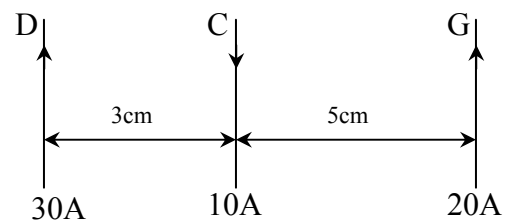
$$B_x = 2.5 + 2.24 \cos \theta = 4.5 \mu T$$

$$B_y = 2.24 \sin \theta = 1 \mu T$$

$$\vec{B} = (4.5\hat{i} + 1\hat{j}) \mu T$$

10. Three long parallel wires carry currents as shown in the figure below. Find the magnitude of the force experienced by a 25cm length of wire C.

(3 points)



$$B_D = \frac{\mu(30A)}{2\pi(0.03)} = 2 \times 10^{-4} T$$

$$B_G = \frac{\mu(20A)}{2\pi(0.05)} = 0.8 \times 10^{-4} T$$

$$B = 2 \times 10^{-4} - 0.8 \times 10^{-4} = 1.2 \times 10^{-4} T$$

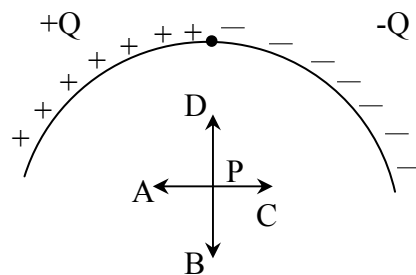
$$F = ILB \sin \theta = 3 \times 10^{-4} N$$

## Part – II

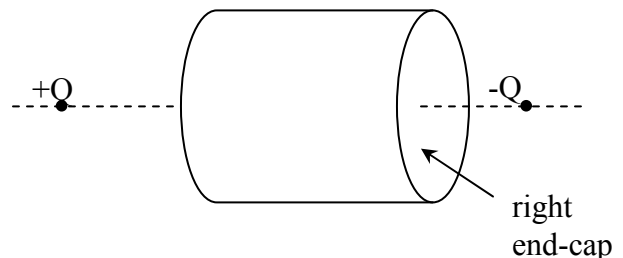
Each question carries one point.

1. A moving charge
  - a. is actually an electric current.
  - b. produces an electric field.
  - c. produces a magnetic field.
  - d. all of the above.
2. Which of the following does NOT produce a magnetic field?
  - a. A varying current-carrying wire
  - b. A moving electric charge
  - c. A stationary electric charge
  - d. A closed electric circuit consisting of an emf source & a resistor.

3. As shown in the figure, an insulating rod is bent into the shape of a semi-circle. The left half has a charge  $+Q$  uniformly distributed along its length & the right half has a charge  $-Q$  similarly distributed. What vector shows the correct direction of the electric field at the center P?
  - a. A
  - b. B
  - c. C
  - d. D
  - e. There is no electric field at P.



4. Positive & negative point charges of equal magnitude lie along the symmetry axis of a cylinder & their distances from the nearest end-caps are equal. What is the sign of the flux through the right end-cap?
  - a. Positive
  - b. Negative
  - c. There is no flux through the right end-cap.



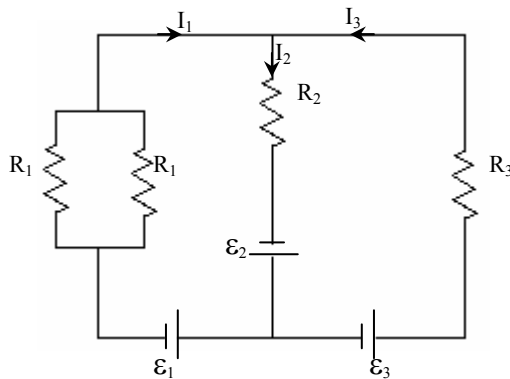
5. A very large horizontal insulating plane is uniformly & negatively charged. The magnitude of the electric field at 0.1m from the plane is  $2.5 \times 10^5$  N/C. What is the surface charge density of the plane?
  - a.  $-3.2 \times 10^{-6} \text{ C/m}^2$
  - b.  $-3.5 \times 10^{-6} \text{ C/m}^2$
  - c.  $-3.9 \times 10^{-6} \text{ C/m}^2$
  - d.  $-4.1 \times 10^{-6} \text{ C/m}^2$
  - e.  $-4.4 \times 10^{-6} \text{ C/m}^2$

6. Which of the following equations is NOT a valid Kirchoff loop equation for the circuit?

✓ a.  $\varepsilon_1 - \varepsilon_2 + I_2 R_2 + I_1 R_1 = 0$

b.  $\varepsilon_1 + \varepsilon_3 - I_3 R_3 + \frac{1}{2} I_1 R_1 = 0$

c.  $\varepsilon_2 + \varepsilon_3 - I_3 R_3 - I_2 R_2 = 0$



7. In a velocity selector, electric & magnetic fields are perpendicular to each other, & the electric & magnetic forces on a charged particle cancel if  $\vec{E} + \vec{v} \times \vec{B} = 0$ . Which of the following conditions on the direction of the velocity  $\vec{v}$  can result in zero net force on the particle, assuming  $\vec{E}$  &  $\vec{B}$  are both non-zero?

a.  $\vec{v}$  parallel to  $\vec{E}$

b.  $\vec{v}$  parallel to  $\vec{B}$

✓ c.  $\vec{v}$  parallel to  $\vec{E} \times \vec{B}$

d. All of the above.

e. None of the above.

8. Many computer keyboard buttons are constructed of parallel – plate capacitors. When a key is pushed down, the soft insulator between the movable plate & the fixed plate is compressed. When a key is pressed down, the capacitance

✓ a. increases

b. decreases

c. remains the same

d. changes in a way that we cannot determine because the electric circuit connected to the keyboard may cause a change in a potential difference.

9. Consider two long, straight wires separated by 1m. In the figure below, the current through wire one is 1 A & is directed out of the plane of the page. Wire two is observed to be attracted toward wire one with a force per unit length of  $2 \times 10^{-7}$  N/m. The current in wire two is

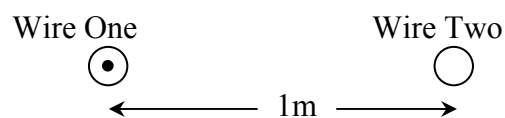
✓ a. 1 A out of page

b. 1 A into page

c. 2 A into page

d. 2 A out of page

e. 3 A out of page





10. Four long straight wires carry equal currents. The wires are parallel & pass through the corners of a square. The directions of the currents are shown in the figure. What is the direction of the net magnetic field at point P, the center of the square?

- a. Toward the top of the page.
- b. Toward the bottom of the page.
- c. Toward the left.
- ✓ d. Toward the right.
- e. Out of the plane of the page.
- f. Into the plane of the page.

