

Physics 101  
 Second Midterm Examination  
 Monday, April 29, 2002  
 5-7 PM

حل نموذجي

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For use by instructors only

Problem	1	2	3	4	5	6	7	8	9	10	Total
Points											

Notes

1. Answer all questions
2. Each question will be assigned 2 points
3. The solution should be given explicitly for each problem
4. No solution = no points
5. Check the correct answer for each question
6. Take  $g = 10 \text{ m/s}^2$

P1- The pilot of an airplane flies  $39^\circ$  north of east with a speed of  $80 \text{ km/h}$  relative to the ground in a wind blowing  $40 \text{ km/h}$  towards the east. What is the velocity (in unit vector notation) of his airplane relative to the wind?

- (a)  $(40\hat{i} + 80\hat{j}) \text{ km/h}$  (b)  $(40\hat{i} - 80\hat{j}) \text{ km/h}$  (c)  $(50.34\hat{i} + 22.17\hat{j}) \text{ km/h}$   
 (d)  $(22.17\hat{i} + 50.34\hat{j}) \text{ km/h}$  (e) other

The General Equation:  $\vec{v}_{pw} = \vec{v}_{pg} + \vec{v}_{gw}$

$$\begin{aligned} \therefore v_{pw} &= 80(\cos 39^\circ)\hat{i} + 80(\sin 39^\circ)\hat{j} + (-40)\hat{j} \quad (\text{where } \vec{v}_{gw} = -\vec{v}_{wg}) \\ &= 62.17\hat{i} - 40\hat{j} + 50.34\hat{j} \\ &= [22.17\hat{i} + 50.34\hat{j}] \text{ m/s} \quad \# \end{aligned}$$

P2- A  $0.2\text{-kg}$  pendulum bob is held at an angle  $\theta$  from the vertical by a  $2\text{-N}$  horizontal force

$\vec{F}$  as shown. The tension in the string supporting the bob (in Newtons) is

- (a)  $\cos \theta$  (b)  $2/\cos \theta$  (c)  $2\sqrt{2}$  (d)  $1$  (e) other

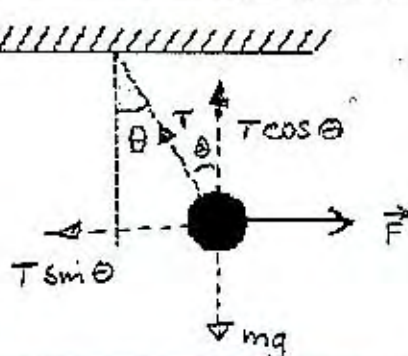
(X)  $F - T \sin \theta = 0 \Rightarrow F = T \sin \theta$

(Y)  $T \cos \theta - mg = 0 \Rightarrow mg = T \cos \theta$

divide both equations:  $\frac{T \sin \theta}{T \cos \theta} = \frac{F}{mg}$

$\Rightarrow \theta = \tan^{-1} \frac{F}{mg} = \tan^{-1} 1 = 45^\circ$

$\therefore T \cos 45^\circ = (0.2)(10) \Rightarrow T = \frac{2}{\cos 45^\circ} = 2\sqrt{2}$



P3- An  $80 \text{ kg}$  person is parachuting and experiencing a downward acceleration of  $2.5 \text{ m/s}^2$ . The mass of the parachute is  $5.0 \text{ kg}$ . What is the upward force on the open parachute from the air?

- (a)  $637.5 \text{ N}$  (b)  $1062.5$  (c)  $850 \text{ N}$  (d)  $250 \text{ N}$  (e)  $-850 \text{ N}$  (f) other

- Total mass  $80 + 5 = 85 \text{ kg}$

- Newton's Second Law  $F_{\text{net}} = ma$

$\Rightarrow F_{\text{air}} - mg = ma$  where  $a = -2.5$  (down)

$F_{\text{air}} = m(g - a) = 85(10 - 2.5) = 637.5 \text{ N}$



P4- A pilot of mass  $90 \text{ kg}$  executes a looping-the-loop maneuver makes a vertical loop of  $3000 \text{ m}$  radius with a speed of  $720 \text{ km/h}$ . Determine the force (in Newtons) exerted by the seat on the pilot at the top of the loop.

- (a)  $900 \text{ N}$  (b)  $600 \text{ N}$  (c)  $300 \text{ N}$  (d)  $0 \text{ N}$  (e) other

from the figure we see that  $N$ ,  $mg$  and  $\frac{v^2}{R}$  have minus sign because they are all inward

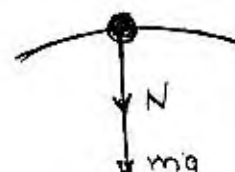
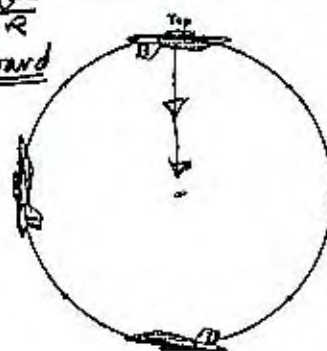
$\Rightarrow$  Newton's Second Law

$-N - mg = m\left(\frac{-v^2}{R}\right)$  multiply by  $-1$

$\Rightarrow N = m\left(\frac{v^2}{R} - g\right)$

But  $v = \frac{720 \times 1000}{3600} = 200 \text{ m/s}$

$\therefore N = 90\left(\frac{(200)^2}{3000} - 10\right) = +300 \text{ N} \quad \#$



P5- Two blocks of masses  $m_1 = 20 \text{ kg}$  and  $m_2 = 40 \text{ kg}$  are pulled up along a rough incline with a force  $\vec{F}$  as shown in the Figure. If  $\mu_k = 0.3$ ,  $\theta = 37^\circ$  and  $T = 168 \text{ N}$ , then the magnitude of the force  $\vec{F}$  is

- (a) 336 N (b) 504 N (c) 436 N (d) 240 N (e) 168 N (f) other

$\sin 37^\circ \approx 0.6$        $\cos 37^\circ \approx 0.8$

or  $m_1$

(X)  $T - m_1 g \sin \theta - f_k = m_1 a$        $f_k = \mu_k N_1$

(Y)  $N_1 = m_1 g \cos \theta \approx 160 \text{ N}$

$\therefore a = \frac{T - m_1 g \sin \theta - \mu_k N_1}{m_1}$

$a = \frac{168 - (20 \times 10 \times 0.6) - (0.3 \times 160)}{20} = 0$

or  $m_2$

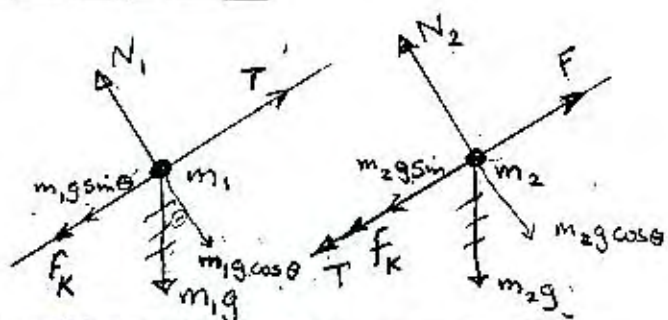
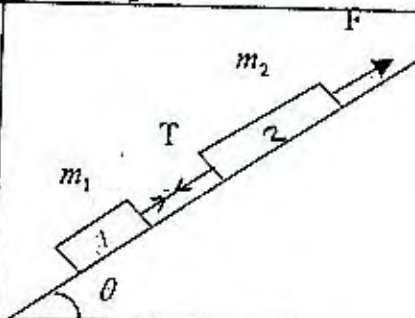
(X)  $F - m_2 g \sin \theta - f_k - T = m_2 a$

(Y)  $N_2 = m_2 g \cos \theta \approx 320 \text{ N}$

$\Rightarrow F = T + f_k + m_2 g \sin \theta$

$F = 168 + (0.3 \times 320) + (40 \times 10 \times 0.6)$

$F = 504 \text{ N} \#$



P6- What is the work  $W_F$  needed to push a 1000-kg box by a force  $F$  for 300 m up a smooth-incline ( $\theta = 17.5^\circ$ ) with constant speed of 5 m/s.

- (a)  $2.86 \times 10^6 \text{ J}$  (b)  $9 \times 10^5 \text{ J}$  (c) 0 J (d) 286 kJ (e) other

Speed is constant means  $a = 0$

$\Delta K$  also is = zero

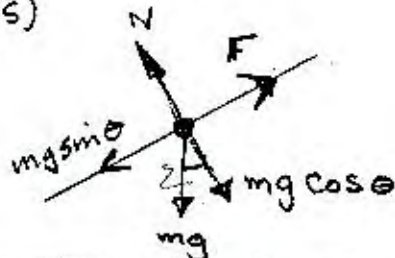
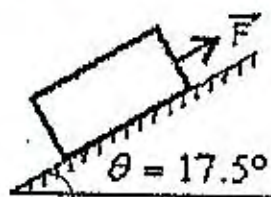
But  $W_F = F \cdot d \cdot \cos \phi$  where  $\phi = 0$

Using Newton's Law.

(X)  $F - mg \sin \theta = 0 \Rightarrow F = (1000)(10)(\sin 17.5^\circ)$

$F = 3007 \text{ N}$

$\therefore W_F = (3007)(300) = 9.02 \times 10^5 \text{ J} \#$



P7- A 2.0-kg body starts moving at  $x = 0$  along the x axis with initial velocity  $v_i = 5.0 \text{ m/s}$ .

The only force acting on the body is  $F_x = -(4x) \text{ N}$ , where  $x$  is in m. For what value of  $x$  will this object first come (momentarily) to rest?

- (a) 4.2 m (b) 3.5 m (c) 5.3 m (d) 6.4 m (e) 5.0 m (f) other

$\Rightarrow$  using variable force Law  $W = \int F(x) dx$

also we know  $W = \Delta K = K_f - K_i$

$\Rightarrow 0 - \frac{1}{2} m v_i^2 = \int_0^x (-4x) dx$

$-\frac{1}{2} (2) (5^2) = \left[ -\frac{4x^2}{2} \right]_0^x$

$-25 = -2x^2$

$x^2 = \frac{25}{2} \Rightarrow x = 3.53 \text{ m} \#$

P8. The position of a 1-kg block moving in the xy plane is given by  $\vec{r} = (t^3 - 2t^2)\hat{i} + 4t^2\hat{j}$ , with r meters and t (>0) in seconds. Find the power delivered to the block by a single acting force  $\vec{F}$  at t = 2s.

- (a) 228 W (b) 200 W (c) 180 W (d) 160 W (e) other

$$\text{Power} = \vec{F} \cdot \vec{v} = m \vec{a} \cdot \vec{v}$$

$$\Rightarrow \vec{v} = \frac{d\vec{r}}{dt} = (3t^2 - 4t)\hat{i} + 8t\hat{j} \quad \text{also } \vec{a} = \frac{d\vec{v}}{dt} = (6t - 4)\hat{i} + 8\hat{j}$$

$$\Rightarrow \text{Power at } 2s = 1 \cdot \vec{a}(2) \cdot \vec{v}(2) = [(6(2) - 4)\hat{i} + 8\hat{j}] \cdot [(3(2)^2 - 4(2))\hat{i} + 8(2)\hat{j}]$$

$$P = [8\hat{i} + 8\hat{j}] \cdot [4\hat{i} + 16\hat{j}] = (32) + (128) = 160 \text{ W} \quad \#$$

Scalar

P9. A block of mass m = 4-kg slides with a velocity  $v_i = 5 \text{ m/s}$  over a frictionless surface towards a spring with spring constant K = 8000 N/m. During its journey it passes over 2 meters of a rough region with  $\mu_k = 0.5$  as shown in the figure. The maximum compression of the spring is

- (a) 2 cm (b) 5 cm (c) 4 cm (d) 10 cm (e) other

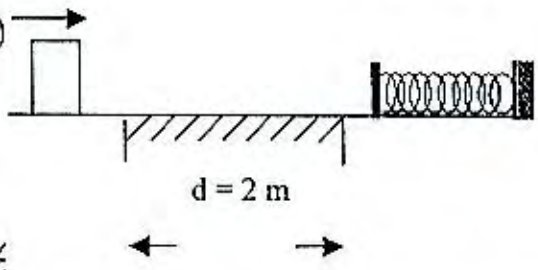
$$\Delta E = W_f$$

$$E_f - E_i = -\mu_k N d \quad v_i = 5 \text{ m/s} \quad K = 8000 \text{ N/m}$$

$$\frac{1}{2} K x^2 - \frac{1}{2} m v_i^2 = -(5)mg(2)$$

$$\frac{1}{2}(8000)x^2 - 50 = -40$$

$$x^2 = \frac{10}{4000} = 2.5 \times 10^{-3}$$

$$x = 0.05 \text{ m} = 5 \text{ cm} \quad \#$$


P10 - A 2-kg block starts to slide down a smooth incline for a distance  $d_1 = 2 \text{ m}$  with initial velocity of 4 m/s. The block continues motion on a rough horizontal surface whose coefficient of kinetic friction  $\mu_k = 0.4$  for a distance  $d_2 = 2 \text{ m}$ . Determine the maximum height ( $h_{\max}$ ) of the block as it travels along the second smooth incline [ $\theta = 37^\circ$  for both inclines].

- (a) 1.8 m (b) 1.2 m (c) 0 m (d) 1.53 m (e) 0.6 (f) other

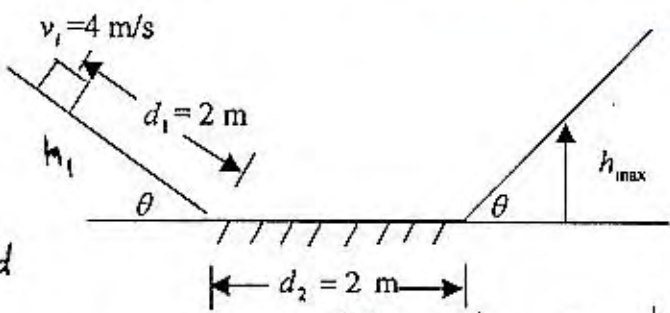
$$\Delta E = W_f$$

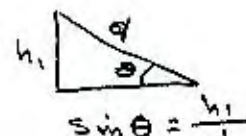
$$E_f - E_i = -\mu_k N d$$

$$[mgh_{\max}]_f - [\frac{1}{2}mv_i^2 + mgh_1]_i = -(0.4)(2)(10)(2)$$

$$10 h_{\max} - \frac{1}{2}(4)^2 - 10(1.2) = -(0.4)(1.2)(10)$$

$$10 h_{\max} - 8 - 12 = -8$$

$$h_{\max} = \frac{20 - 8}{10} = \frac{12}{10} = 1.2 \text{ m} \quad \#$$




$$\sin \theta = \frac{h_1}{d}$$

$$h_1 = d \sin \theta$$

$$h_1 = 1.2 \text{ m}$$